

Indian Buffet Processes with Power-law Behavior

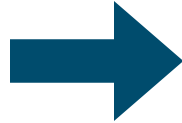
Paper 464
Poster T20

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IBPs:

Bayesian nonparametric latent variable models with an infinite number of latent variables.



This paper:

A three parameter generalization of IBPs with power-law behavior.



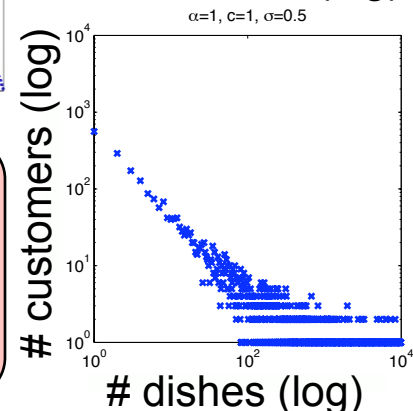
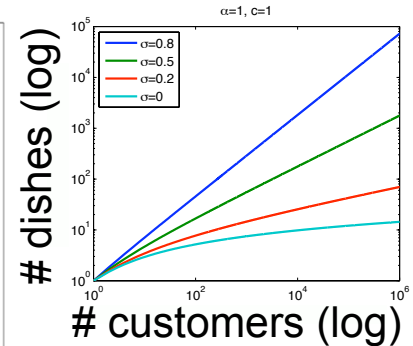
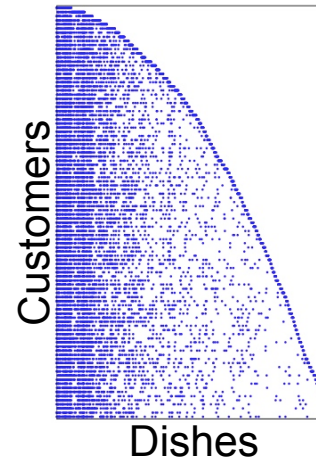
Power-law:

Many natural phenomena exhibit power-law properties.

IBP with parameters $\alpha > 0$, $c > -\sigma$, $0 \leq \sigma < 1$.

- Customer 1 tries $\text{Poisson}(\alpha)$ dishes;
- Customer $n+1$:
 - tries dish k with probability $\frac{m_k - \sigma}{n + c}$;
 - $m_k = \#$ customers who tried dish k .
 - tries $\text{Poisson}\left(\alpha \frac{\Gamma(1+c)\Gamma(n+c+\sigma)}{\Gamma(n+1+c)\Gamma(c+\sigma)}\right)$ new dishes.

$\alpha=100, c=1, \sigma=0.5$



Infinitely exchangeable. The de Finetti measure is a completely random measure called **stable-beta process**.

Representations: IBP, stable-beta, stick-breaking, size-biased.

Applied to modelling word occurrences in documents