



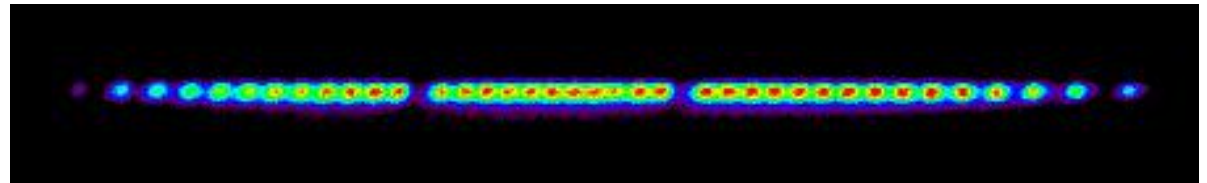
Universal low-rank matrix recovery from Pauli measurements

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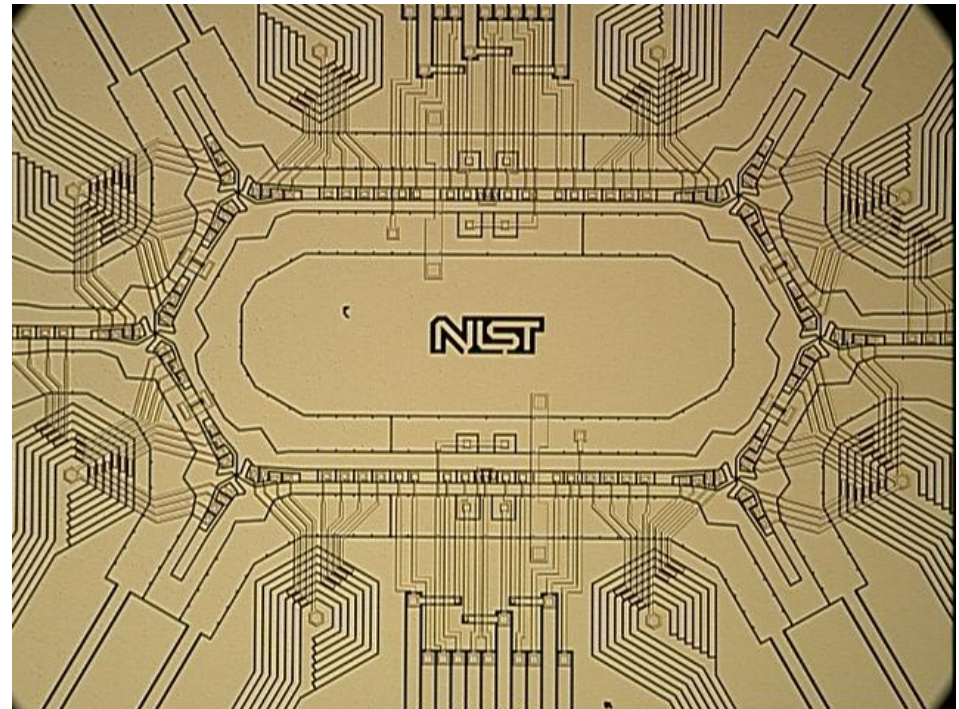
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Motivation: experiments with complex quantum systems

- Ion traps



- Small quantum computers
- Precision metrology
- Simulating chemical dynamics
- Want to scale up: 10 to 100 qubits





Quantum state tomography

- Characterizing an unknown quantum state: want to learn the *density matrix* ρ in $\mathbb{C}^{d \times d}$
 - For a state of n qubits, $d = 2^n \Rightarrow$ pretty big!
 - In many cases, ρ has rank $r \ll d$
- Choose measurement matrices P_1, P_2, \dots
- Observe $\text{Tr}(P_1\rho), \text{Tr}(P_2\rho), \dots$
 - Use Pauli matrices – matrix analogue of Fourier basis
 - **Use compressed sensing techniques!**



Our results

- There is a **universal** set of $O(rd \log^6 d)$ Pauli measurements, that can be used to reconstruct any rank- r state ρ in $\mathbb{C}^{d \times d}$
 - Choose random Pauli matrices, use the matrix Lasso
 - Get strong (near-optimal) error bounds [CP'11]
- Random Pauli measurements obey the **restricted isometry property (RIP)**
 - Embed the manifold of low-rank matrices into $O(rd \log^6 d)$ dimensions
 - More structured, less random than a Gaussian random projection